



First session on ***GPS and Galileo Data Processing: from fundamentals to precise navigation*** Lecture Notes(*)

(*) Partially based on

“Global Positioning System; Signals, Measurements, and Performance”, P. Misra and P. Enge, Ganga-Jamnua Press, 2004 and on

“GPS data processing: code and phase. Algorithms, techniques and recipes”, M.Hernández-Pajares, J.M. Juan, J.Sanz, 2001-2005.

Manuel Hernández-Pajares

UPC-IonSAT res. group

[contact e-mail : manuel@ma4.upc.edu]

<https://scholar.google.es/citations?user=Tm-DcsMAAAAJ&hl=en>

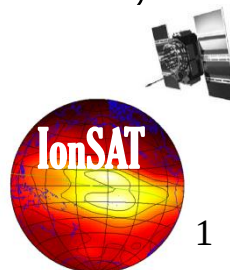
With contributions from M. Hernández-Pajares, J.M.Juan, J.Sanz, M. García-Fernández, R. Orús-Pérez, P.Ramos, A. Aragón-Ángel, D.Salazar, A.García-Rigo, among others

*Technical University of Catalonia (UPC)
E08034-Barcelona, Spain*



UNIVERSITAT POLITÈCNICA
DE CATALUNYA
BARCELONATECH

Hernández-Pajares et al.



Main Goal: To acquire GPS Fundamental Background & Processing skills

OUTLINE

0. Introduction to Navigation

I. Introduction to Space Geodesy

1.1 Space Geodesy

1.2 Basic concepts of Satellite Geodesy

1.3 Historical Development of Satellite Geodesy

1.4 Applications of Satellite Geodesy

II. Global Positioning System (GPS)

2.1 Introduction

2.2 Space Segment

2.3 Control Segment

2.4 Observation Principle and Signal Structure



III. Satellite Orbital Motion

3.1 Two-Body Problem

3.2 Elliptic motion of the satellite

3.3 Orbital elements

3.4 Perturbed Satellite Motion

IV. Physical fundamentals

4.1 Reference Coordinate Systems

4.2 Time

4.3 Electromagnetic signal propagation

V. GPS observations and data processing

5.1 Observables

5.2 GPS point positioning

5.3 Differential GPS positioning

VI. Some applications of GPS

VII. GALILEO and applications

Bibliography:

Hernández-Pajares, M. et al., *Introduction to GNSS Data Processing*, 1998-2015 <http://newg1.upc.es/lectures/legad/>

Hernández-Pajares, M., J.M. Juan, J.Sanz, *GPS data processing: Code and Phase Algorithms, Techniques and Recipes*, 2002-2008, http://newg1.upc.es/lectures/legad/docs/LeGAD-00.Book-English_v8b.pdf

Hofmann-Wellenhof, Lichtenegger and Wasle, *GNSS, Global Navigation Satellite Systems, GPS, GLONASS, Galileo and more*, Springer, Wien, New York, 2008.

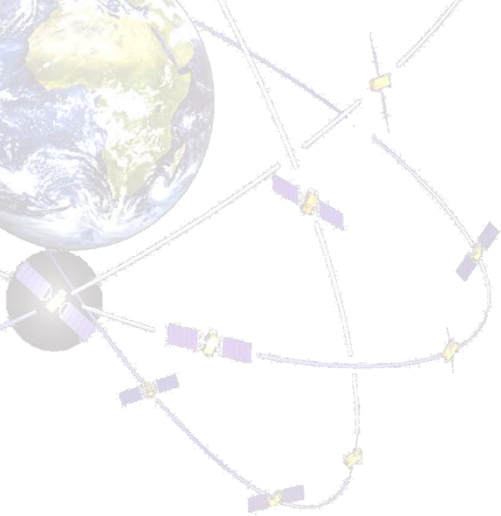
P. Misra and P. Enge, *Global Positioning System; Signals, Measurements, and Performance*, Ganga-Jamnua Press, 2004.

Parkinson B.W., J.J.Spilker (eds), *Global Positioning System: Theory and Applications, Vols. I & II*, Progress in Astronautics and Aeronautics, Vol. 163 & 164, 1996.

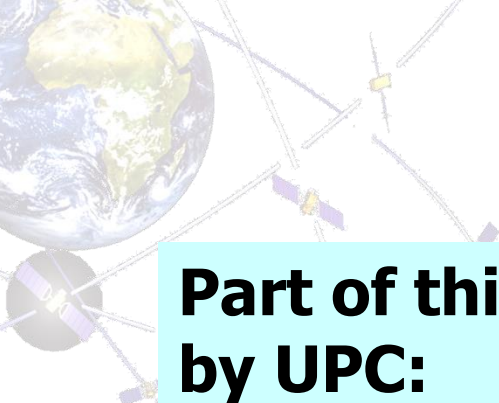
Seeber G., *Satellite Geodesy*, de Gruyter ed., 1993.

GPS World: <http://www.gpsworld.com>

Inside GNSS: <http://www.insidegnss.com/>



Teacher coordinates:
Manuel Hernández-Pajares
Mod. C3, Desp. 209,
Campus Nord UPC
Barcelona, Spain
(manuel@ma4.upc.edu)



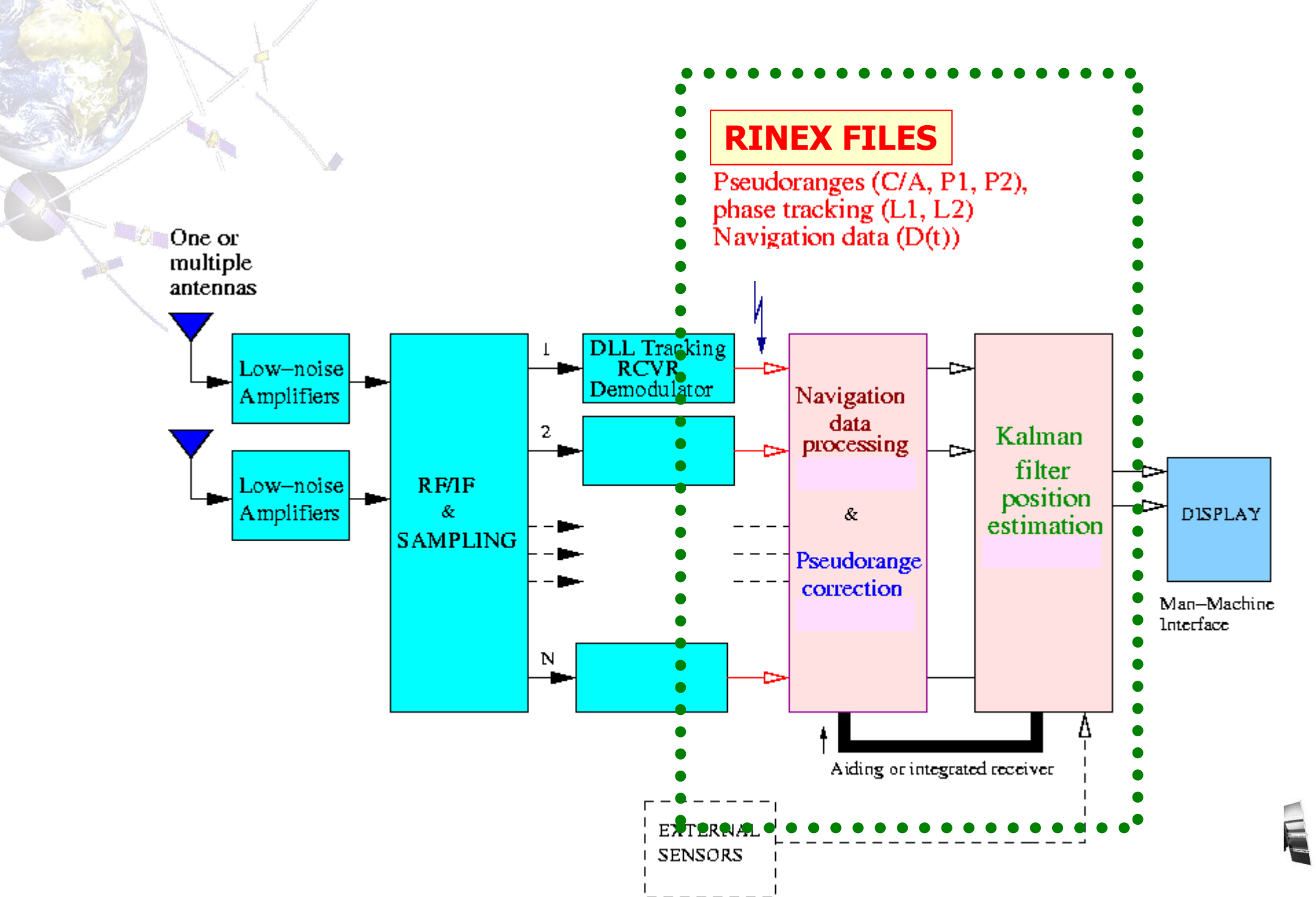
Part of this course is based on the book edited by UPC:

*GPS data processing: code and phase.
Algorithms, techniques and recipes.*

These slides show some exercises and examples whose data files (with actual GPS data) and corresponding software (with source code) are provided in the book.

Summary

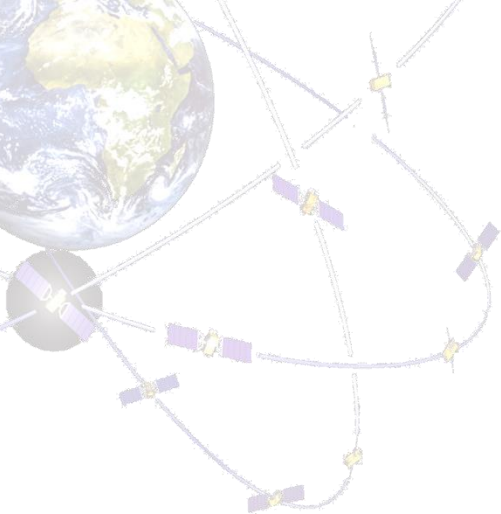
- **Introduction.**
- **GPS measurements and their combinations.**
- **Satellite coordinates.**
- **The model.**
- **Navigation equations.**
- **Code and phase differential positioning.**
 - Floating versus fixing ambiguities.



Specific Objectives:

- To learn about **GPS observables** (code and phase), their characteristics, properties, combinations and applications.
- To learn how to **calculate satellites orbits and clocks** from navigation message. To know the achievable precision.
- To learn how to **model pseudodistance** for code and phase measurements. This includes calculation of: 1) Coordinates at emission epoch, 2) Ionospheric delay (Klobuchar model), 3) Tropospheric delay, 4) relativistic correction, 5) clocks offsets and satellite instrumental delays, 6) phase wind-up, etc.
- To learn how to **set and solve the navigation equation system** using least-squares or Kalman filter (algorithm level).
- To know how to use phase differential positioning: Floating and fixing ambiguities.

**To get tools and skills to process and analyze GPS data.
To implement algorithms for satellite navigation.**

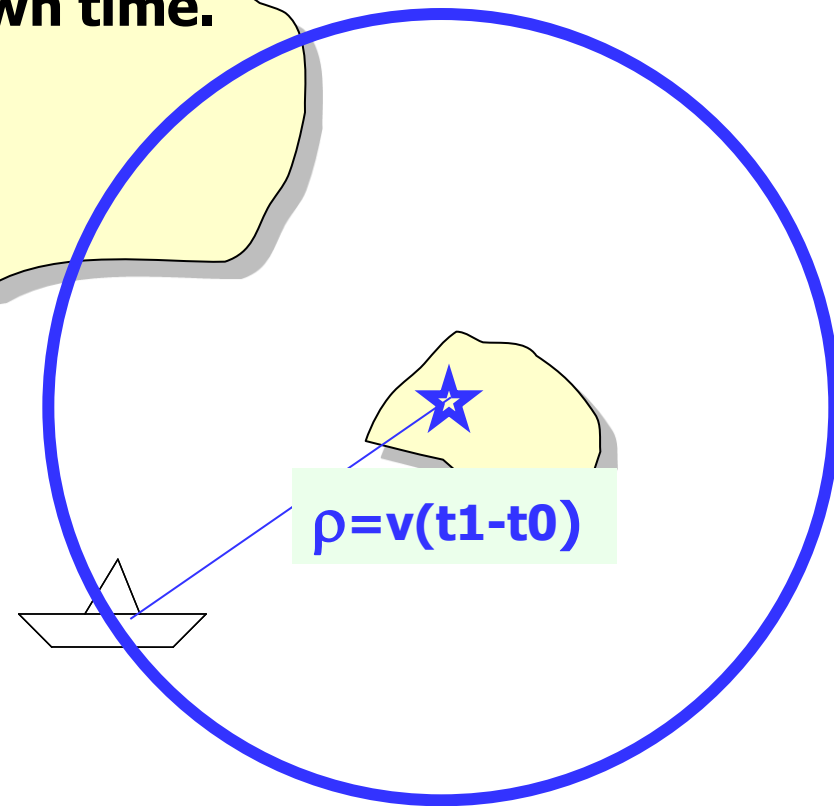


Introduction

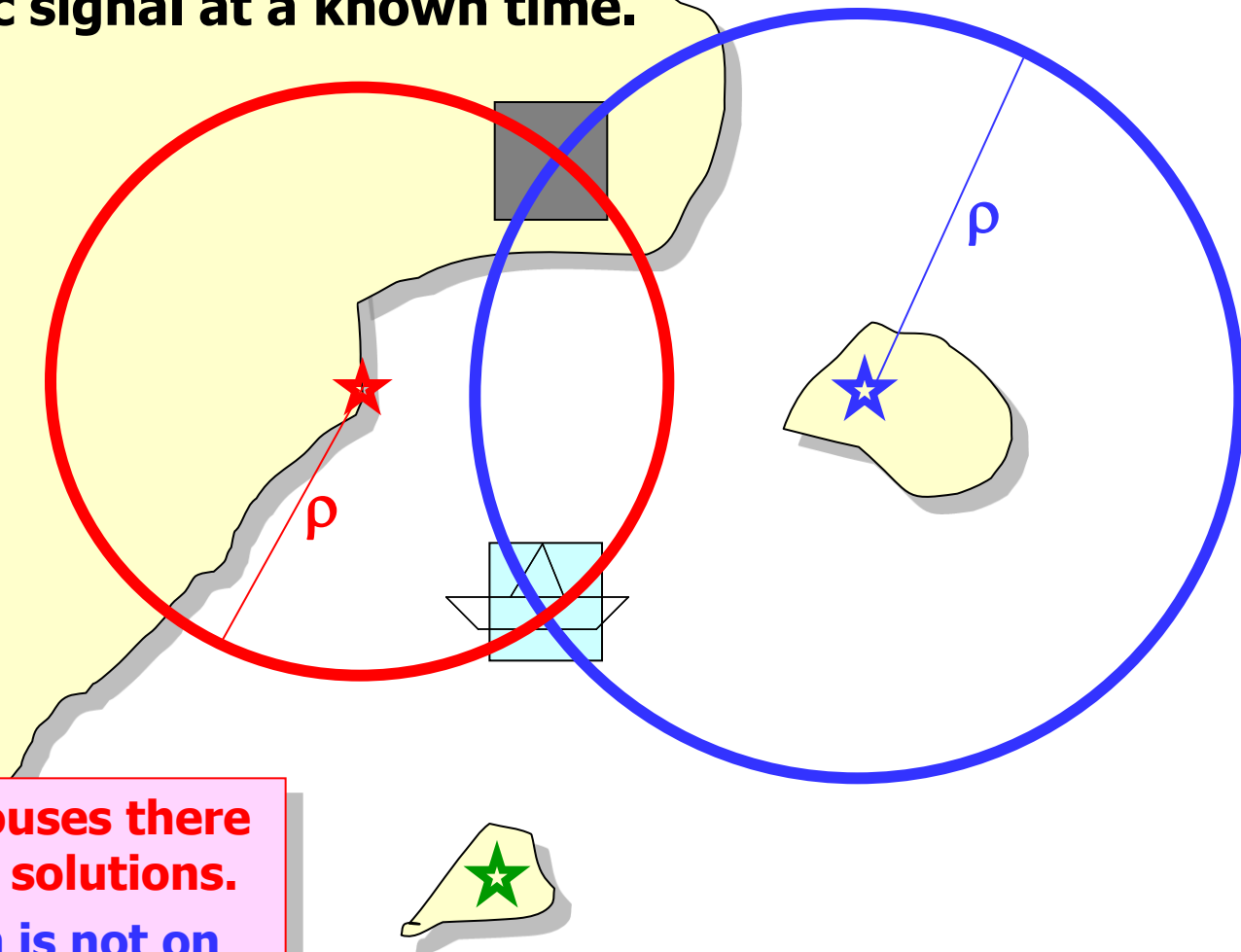
A ship determines its location from a set on lighthouses that send an acoustic signal at a known time.

Knowing the emission time "t0" in the lighthouse and the reception time "t1" in the ship, the traveling time "t1-t0", and the geometric range " $\rho = v(t1 - t0)$ " may be computed.

With only one lighthouse there is a whole circumference of possible locations



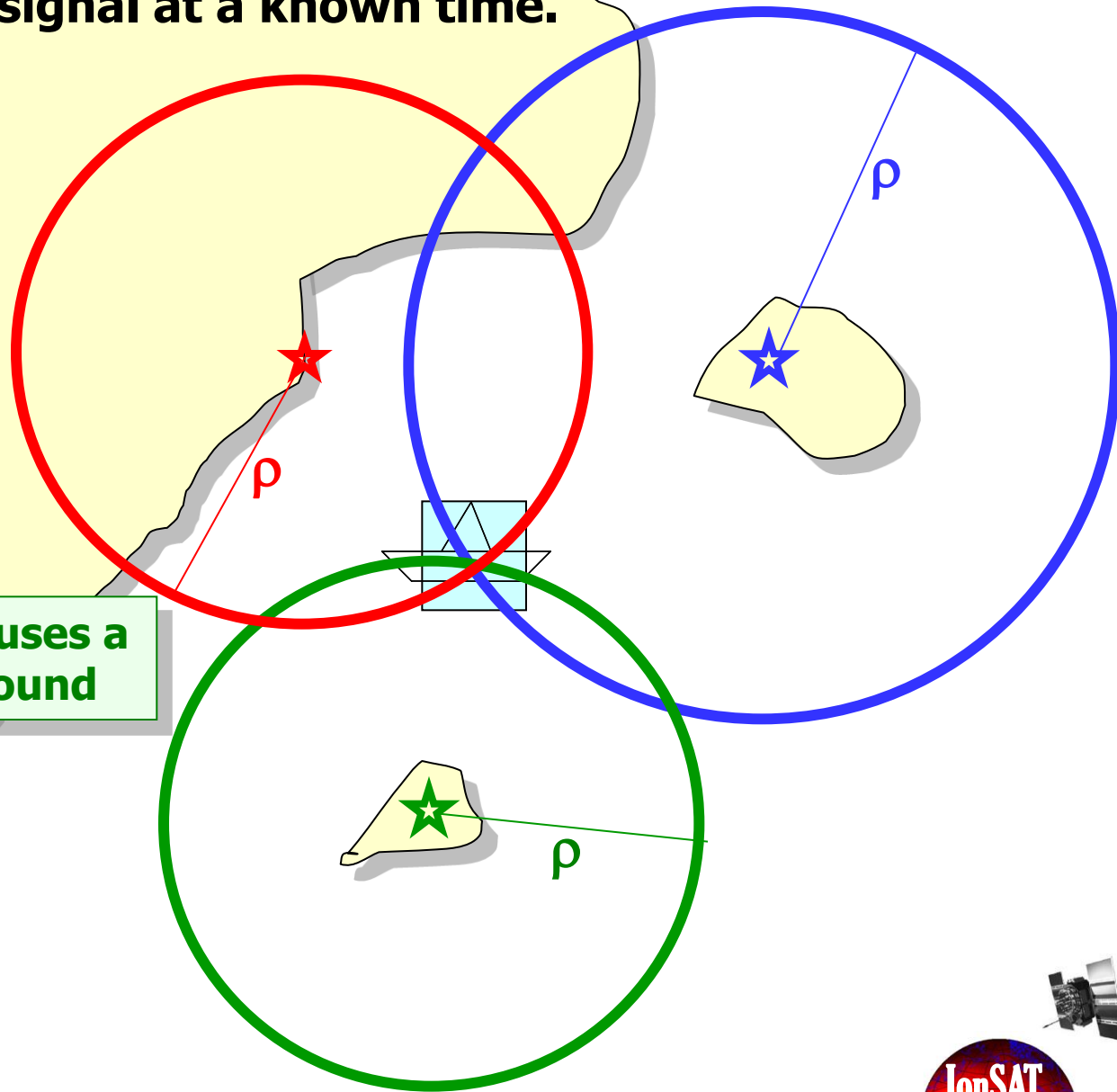
A ship determines its location from a set on lighthouses that send an acoustic signal at a known time.



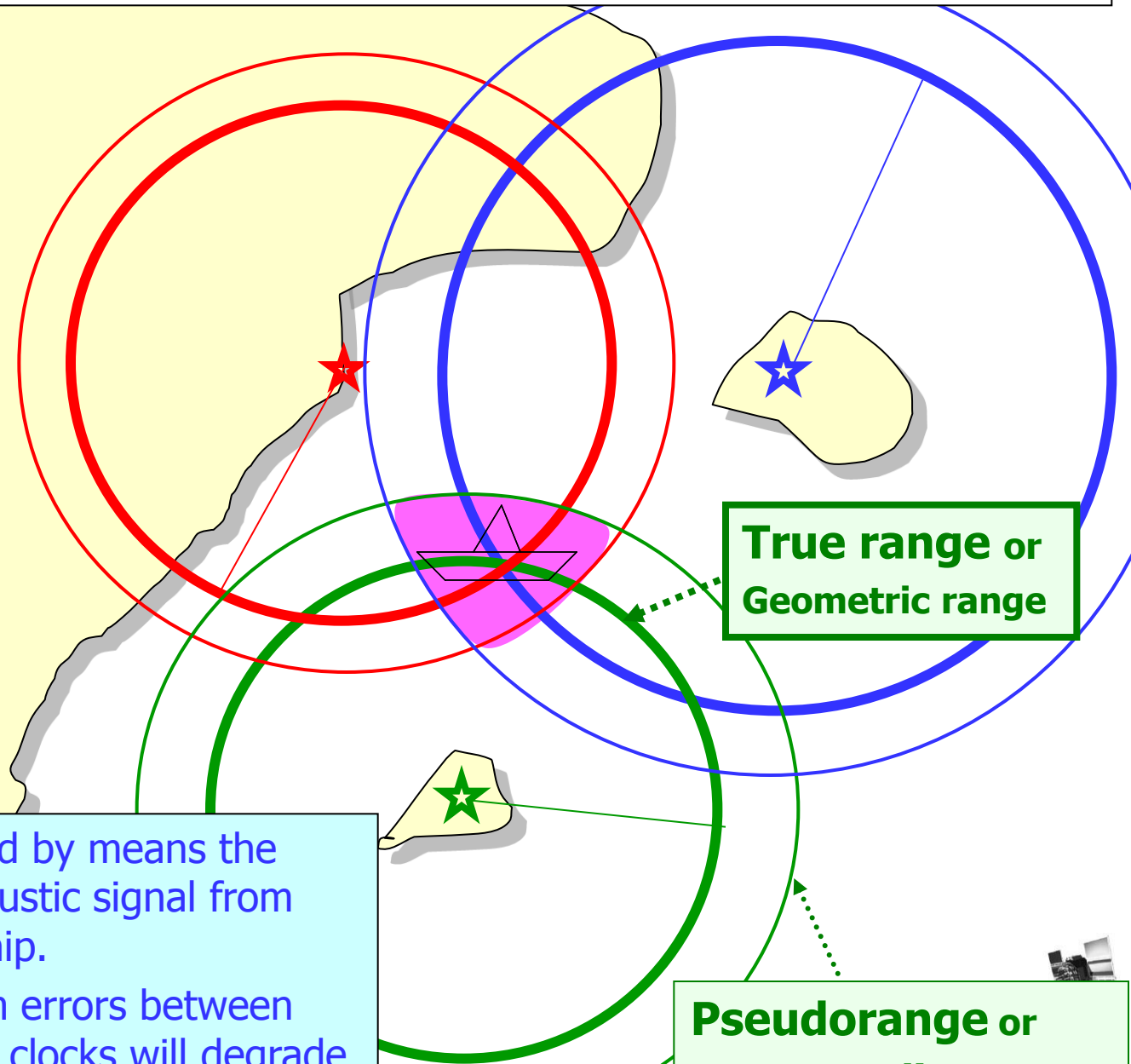
With two lighthouses there are two possible solutions. But, one of them is not on the sea!

A ship determines its location from a set on lighthouses that send an acoustic signal at a known time.

With three lighthouses a single solution is found



Errors in the clocks (lighthouses and ship) synchronism affects the accuracy



The **ranges** are measured by means the **traveling time** of the acoustic signal from the lighthouses to the ship.

Thence, the synchronism errors between the lighthouses and ship clocks will degrade the positioning accuracy.

**True range or
Geometric range**

**Pseudorange or
apparent distance
due to the error clocks**

SUMMARY: The positioning system is based on:

- To know the coordinates of the lighthouses
- To know the ranges from the ship to the lighthouses
- To solve a geometric problem.

NOTE: the **ranges** are measured by means the **traveling time** of the acoustic signal from the lighthouses to the ship.

Thence, the synchronism errors between the lighthouses and ship clocks will degrade the positioning accuracy.

True range or Geometric range

Pseudorange or apparent distance due to the error clock.

How GPS Works

Satellites broadcast orbit and clock data

→ Satellite coordinates and clock offset

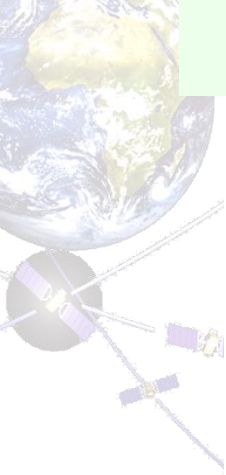
Lighthouses coordinates

Receiver measures traveling time from satellite to receiver
→ Pseudorange (P)

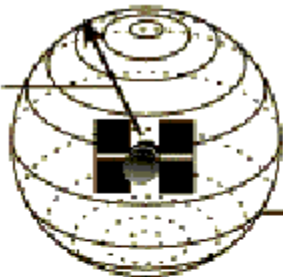
Lighthouses-ship ranges.

Thence, the receiver coordinates are found **solving a geometrical problem**: from sat. coordinates and ranges

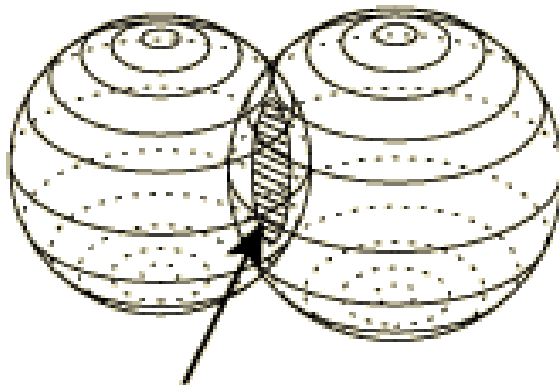
How GPS Works



20.000km

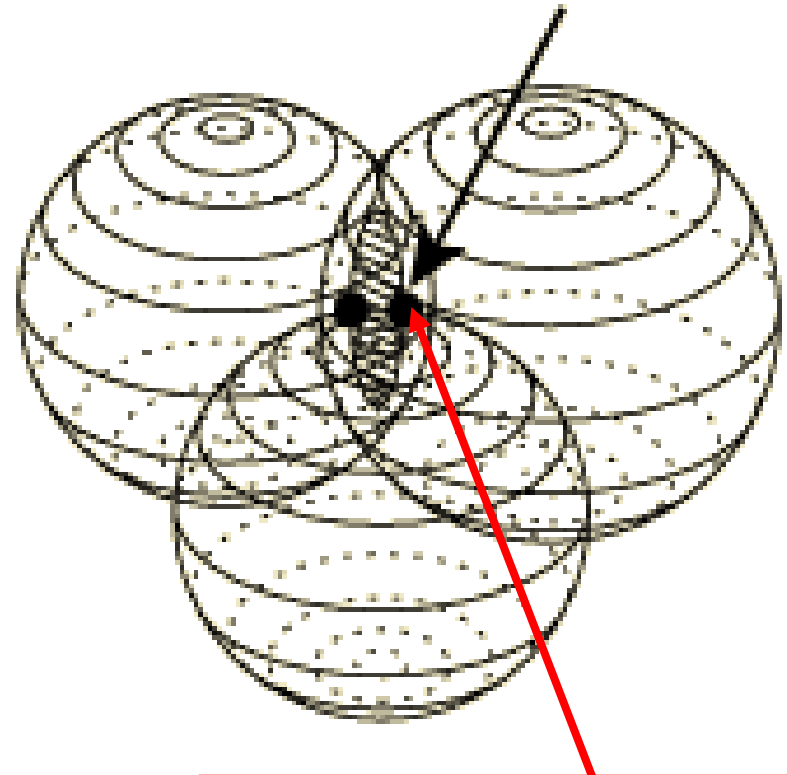


We're somewhere on this sphere.



Two measurements puts us somewhere on this circle

Three measurements puts us at one of two points



One of the solutions is not on the Earth surface.

How GPS Works



How GPS Works

Lesson 3:

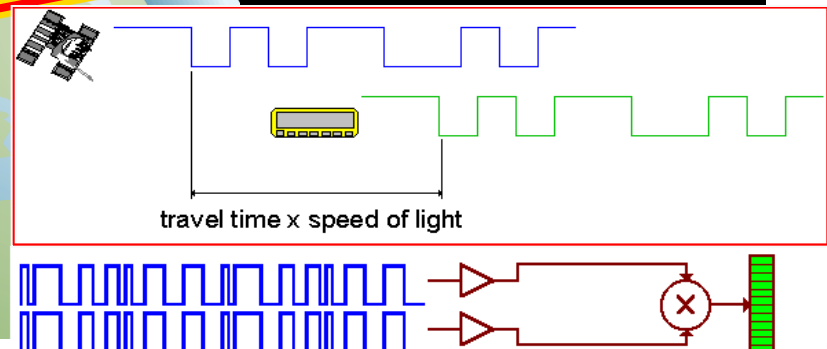
GPS measurements
and its
combination

Measurements: Ranges

"Pseudoranges" are
computed from the
traveling time sat-rec

Several error sources
affect these
measurements

Receiver
location



How GPS Works

Satellite location

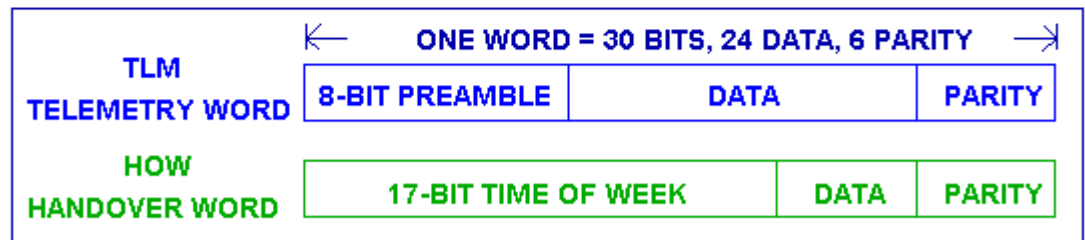
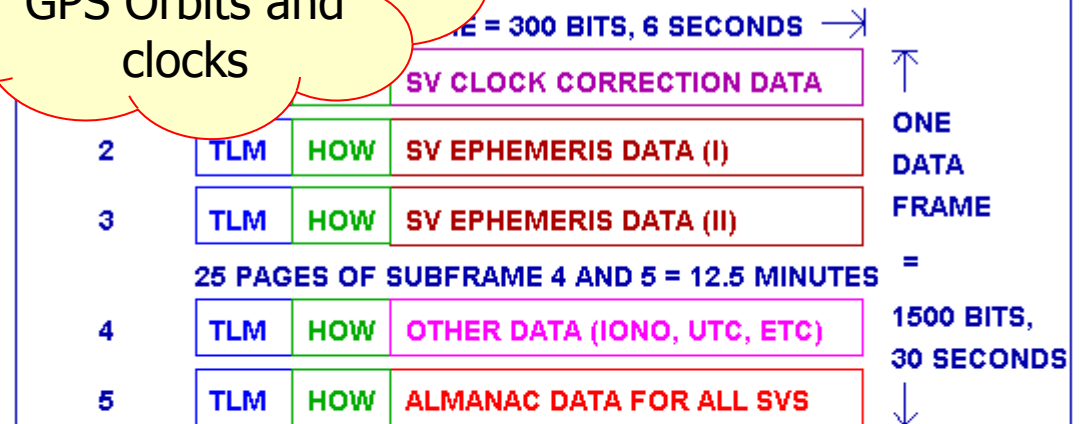
Satellite coordinates and clock offsets are computed from the navigation message: (orbit.f)

Lesson 4:

GPS Orbits and clocks

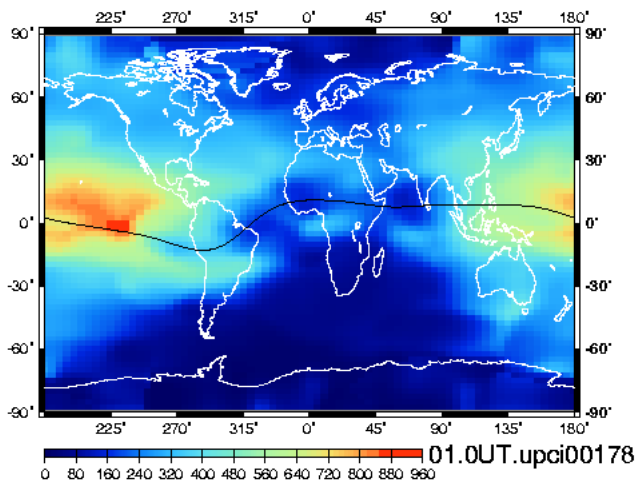


Receiver location

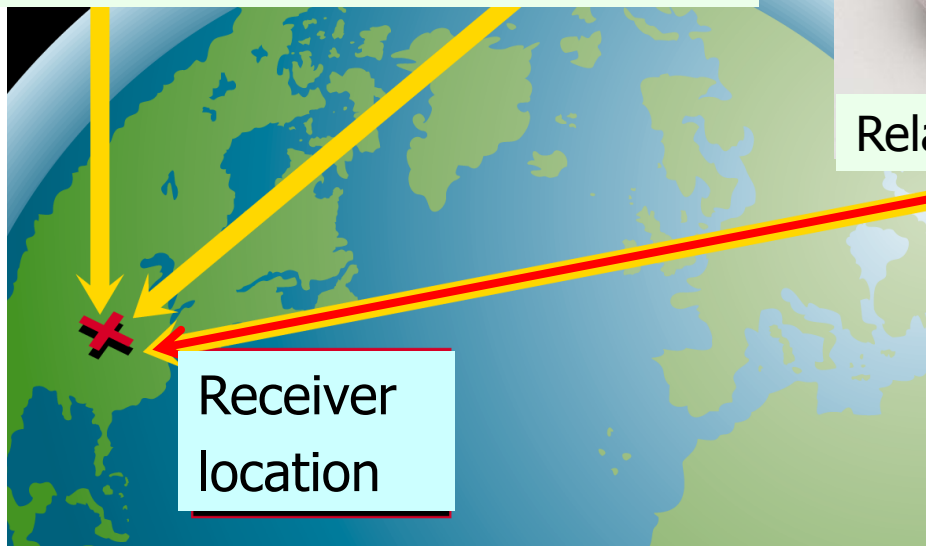


GPS NAVIGATION DATA FORMAT

P HDANA 10/92



Atmospheric propagation: IONO, TROPO



GPS Works



Relativistic

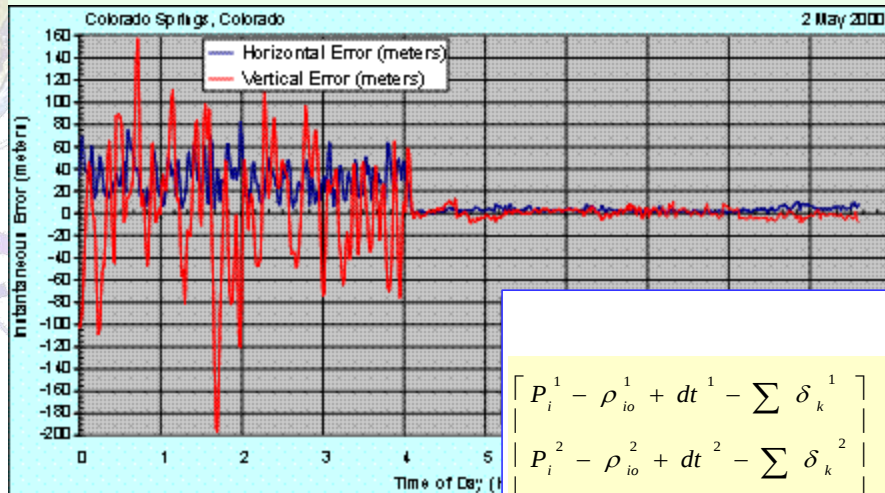
Lesson 5:
GPS measurements
modeling (code)

• MODEL:

Atmospheric propag.,
relativistic effects,
clocks and instrum.
delays are modeled
and removed.

And the navigation
equations are built

How GPS Works



$$\begin{bmatrix} P_i^1 - \rho_{io}^1 + dt^1 - \sum \delta_k^1 \\ P_i^2 - \rho_{io}^2 + dt^2 - \sum \delta_k^2 \\ \dots\dots\dots \\ P_i^n - \rho_{io}^n + dt^n - \sum \delta_k^n \end{bmatrix} =$$

$$\begin{bmatrix} \frac{x_{io} - x^1}{\rho_{io}^1} & \frac{y_{io} - y^1}{\rho_{io}^1} & \frac{z_{io} - z^1}{\rho_{io}^1} & 1 \\ \frac{x_{io} - x^2}{\rho_{io}^2} & \frac{y_{io} - y^2}{\rho_{io}^2} & \frac{z_{io} - z^2}{\rho_{io}^2} & 1 \\ \dots\dots\dots \\ \frac{x_{io} - x^n}{\rho_{io}^n} & \frac{y_{io} - y^n}{\rho_{io}^n} & \frac{z_{io} - z^n}{\rho_{io}^n} & 1 \end{bmatrix}$$

$$\begin{bmatrix} \Delta x_i \\ \Delta y_i \\ \Delta z_i \\ cdt_i \end{bmatrix}$$

Lesson 6:

Solving the navigation Equations

Navigation equations

The geometric problem is linearized, and Weighted Least Mean Squares or Kalman filter are used to compute the solution.

MODEL:

Atmospheric propagation, relativistic effects, clocks and instrument delays are modeled and removed.

And the navigation equations are built

How GPS Works

Lesson 7:

Code and phase
differential positioning.
Floating/fixing
ambiguities

